

26-47. At the instant the switch is closed the charge on each capacitor is zero, so the voltage drop across the capacitor is also zero, and the capacitor acts as a wire—a ‘short circuit’— i.e., zero voltage difference with the current going to charge the capacitor. Resistors connected in parallel to such capacitors draw zero current as $\Delta V = 0$. At long times each capacitor will be saturated, no current will flow through it; it will act as a disconnected wire (‘open circuit’)

- (a) The circuit, with each capacitor replaced with a wire, becomes: $75 + (50 \parallel 25) + 15 = 75 + 50 \cdot 25 / 75 + 15 = 106.67 \Omega$. The current is $I = V/R_{eq} = 100/106.67 = 0.938 \text{ A}$.
- (b) The circuit, with each capacitor deleted, becomes: $25 + 75 + 25 + 25 + 15 = 165 \Omega$. The current is $I = V/R_{eq} = 100/165 = 0.606 \text{ A}$.

26-49. Note that the time constant is $\tau = RC = 0.0147 \text{ s}$, the charging capacitor follows: $q = C\mathcal{E} (1 - e^{-t/\tau})$, the discharging $q = Q_0 e^{-t/\tau}$.

- (a) Note that $t/\tau = .01/0.0147 = 0.6803$:

$$q = C\mathcal{E} (1 - e^{-t/\tau}) = 1.5 \times 10^{-5} \cdot 18 (1 - e^{-0.6803}) = 1.33 \times 10^{-4} \text{ C}$$

- (b) $V_C = q/C = 1.33 \times 10^{-4} / 1.5 \times 10^{-5} = 8.88 \text{ V}$; $V_R = \mathcal{E} - V_C = 9.12 \text{ V}$

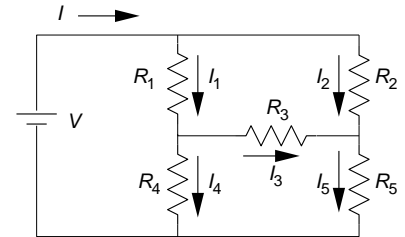
- (c) Both are 8.88 V: the voltage goes up 8.88 V across the capacitor, and down 8.88 V across the resistor.

- (d) For this additional time increment: $t/\tau = .01/0.0147 = 0.6803$:

$$q = Q_0 e^{-t/\tau} = 1.33 \times 10^{-4} e^{-0.6803} = 6.75 \times 10^{-5} \text{ C}$$

26-64. My plan is to use I_1 , I_2 , and I_3 as independent variables and immediately substitute $I_4 = I_1 - I_3$ and $I_5 = I_2 + I_3$ into the loop equations. I’ll use as independent loops the outer loop L_0 , the top loop L_T , and the left loop L_L . The results are (respectively):

$$\begin{aligned} \mathcal{E} - I_2 R_2 - (I_2 + I_3) R_5 &= 0 \\ -I_2 R_2 + I_3 R_3 + I_1 R_1 &= 0 \\ \mathcal{E} - I_1 R_1 - (I_1 - I_3) R_4 &= 0 \end{aligned}$$



I’ll rewrite these in more standard form as:

$$\begin{aligned} \mathcal{E} &= I_2(R_2 + R_5) + I_3 R_5 \\ 0 &= I_1 R_1 - I_2 R_2 + I_3 R_3 \\ \mathcal{E} &= I_1(R_1 + R_4) - I_3 R_4 \end{aligned}$$

Note that a program like *Mathematica* can immediately solve these equations symbolically with a command like:

`Solve[{e==i2(r2+r5)+i3 r5,0==i1 r1-i2 r2+i3 r3,e==i1(r1+r4)-i3 r4},{i1,i2,i3}]`

and result:

$$\frac{e (r_3 r_5 + r_2 (r_3 + r_4 + r_5))}{r_4 (r_3 r_5 + r_2 (r_3 + r_5)) + r_1 ((r_3 + r_4) r_5 + r_2 (r_3 + r_4 + r_5))}$$

$$\frac{e (r_3 r_4 + r_1 (r_3 + r_4 + r_5))}{r_4 (r_3 r_5 + r_2 (r_3 + r_5)) + r_1 ((r_3 + r_4) r_5 + r_2 (r_3 + r_4 + r_5))}$$

$$\frac{e (r_2 r_4 - r_1 r_5)}{r_4 (r_3 r_5 + r_2 (r_3 + r_5)) + r_1 ((r_3 + r_4) r_5 + r_2 (r_3 + r_4 + r_5))}$$

Do notice the important result that $I_3 = 0$ iff $R_2 R_4 = R_1 R_5$ (this condition is more commonly written $R_2/R_5 = R_1/R_4$). However, my calculator needs numbers not letters, so I enter the system of equations:

$$\begin{aligned} 14 &= 3I_2 + I_3 \\ 0 &= I_1 - 2I_2 + I_3 \\ 14 &= 3I_1 - 2I_3 \end{aligned}$$

and find: $I_1 = 6$ A, $I_2 = 4$ A, $I_3 = 2$ A $\Rightarrow I_4 = I_1 - I_3 = 4$ A, $I_5 = I_2 + I_3 = 6$ A and the battery draws: $I = I_1 + I_2 = 10$ A.

The equivalent resistance is easily found from the battery voltage/current: $R = V/I = 14/10 = 1.4 \Omega$.