

Class 3

Survival ch 2

the ellipse has become a line ($e=1$)

#2 $q=20$

$T=20^{3/2} = 89.4 \text{ years}$

large diameter of ellipse = $2q$
but just half = 44.7 years

#3 $q = T^{2/3} = (75.7)^{2/3} = 17.9 \text{ AU}$

$q(1-e) = \text{peri} = .587 \text{ AU}$

$1 - \frac{.587}{q} = e = .967$

#6 $h = rv \sin \theta = (1.6)(1.2) \sin 60^\circ = 1.663$ $\frac{AU^2}{\text{year}} = \sqrt{GM a(1-e^2)}$

$\frac{1}{2} v^2 - \frac{GM}{r} = -\frac{GM}{2a}$

$\frac{1}{r} - \frac{1}{2} \frac{v^2}{GM} = \frac{1}{2a}$

$a = \frac{1}{2 \left(\frac{1}{r} - \frac{1}{2} \frac{v^2}{GM} \right)} = \frac{1}{2 \left(\frac{1}{1.6} - \frac{1}{2} \left(\frac{1.2}{2\pi} \right)^2 \right)}$

$= .824 \text{ AU}$

$\frac{h^2}{GM a} = 1 - e^2$; $e = \sqrt{1 - \frac{h^2}{GM a}} = \sqrt{1 - \frac{(1.663)^2}{2\pi \cdot .824}}$

$= .957$

$\frac{a(1-e^2)}{1+e \cos \phi} = r$

$\frac{a(1-e^2)}{r} = 1+e \cos \phi$

$\frac{1}{e} \left[\frac{a(1-e^2)}{r} - 1 \right] = \cos \phi = \frac{1}{.957} \left[\frac{.824(1-.957^2)}{1.6} - 1 \right] = -.9996$

all sig figs $\rightarrow 178.486$

\downarrow
 178.5°